

Human-Computer Interaction

# Statistics III

Intermediate Inferential Statistics

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# Today's Agenda

- » **Today:** Multifactorial analysis + tutorials using example data
- » **Tuesday:** Writing + tutorials using your data
- » **Reminder:** Please complete course evaluations at AEFIS



COMP SCI 770-001  
2021 Fall

Ends: 12/15/2021 (6 days)



Currently  
In Progress

# Quick tutorial on correlation analysis

r-value

p-value

## Correlation analysis in R

```
cor.test(data$Price,data$Safety)
```

Pearson's product-moment correlation

data: data\$Price and data\$Safety

t = -0.84807, df = 88, p-value = 0.3987

alternative hypothesis: true correlation is not equal to 0

95 percent confidence interval:

-0.2916892 0.1192782

sample estimates:

```
cor  
-0.09003692
```

## Correlation analysis in JMP

The screenshot shows the JMP software interface with the following sections:

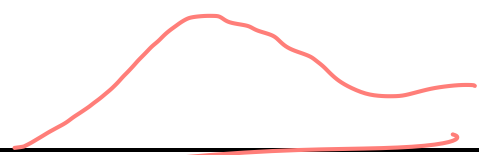
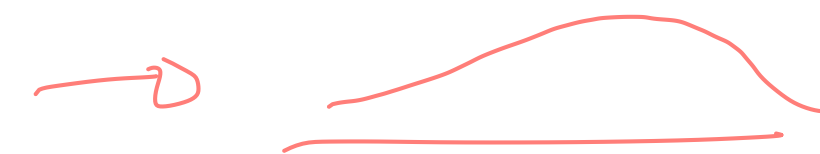
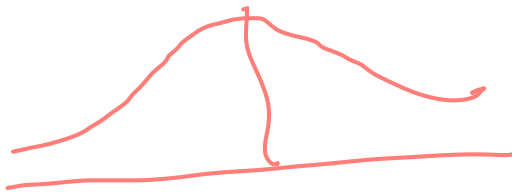

- Multivariate**
  - Correlations**

	Price	Safety
Price	1.0000	-0.0900
Safety	-0.0900	1.0000

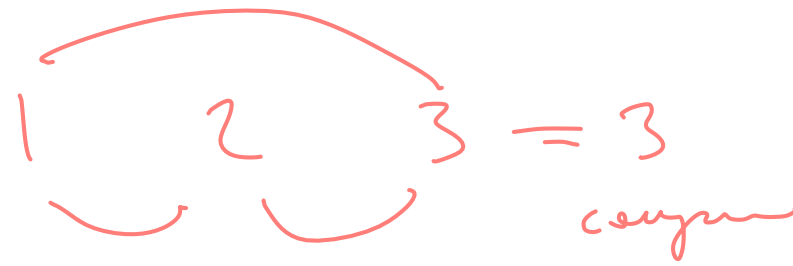
The correlations are estimated by Row-wise method.
  - Correlation Probability**

	Price	Safety
Price	<.0001	0.3987
Safety	0.3987	<.0001
  - Scatterplot Matrix**
  - Pairwise Correlations**

Variable	by Variable	Correlation	Count	Lower 95%	Upper 95%	Signif Prob
Safety	Price	-0.0900	90	-0.2917	0.1193	0.3987

	Nominal	Categorical (2+)	Ordinal	Quantitative Discrete	Quantitative Non-Normal	Quantitative Normal
Nominal	Chi-squared, Fisher's	<del>Chi-squared</del>	Chi-squared Trend, Mann-Whitney	Mann-Whitney	Mann-Whitney, log-rank	<del>Student's t</del>
Categorical (2+)	<del>Chi-squared</del>	<del>Chi-squared</del>	Kruskal-Wallis	Kruskal-Wallis	Kruskal-Wallis	ANOVA
Ordinal	Chi-squared Trend, Mann-Whitney		Spearman rank	Spearman rank	Spearman rank	Spearman rank, linear regression
Quantitative Discrete	Logistic regression			Spearman rank	Spearman rank	Spearman rank, linear regression
Quantitative Non-Normal	Logistic regression				Plot data-Pearson, Spearman rank	Plot data-Pearson, Spearman rank & linear regression
Quantitative Normal	Logistic regression				Linear regression	<del>Pearson</del> , linear regression





Consider this dataset. Can we use multiple t-tests?

Participant ID	Group	Time	Coding
Participant 01	Standard ✓	245	0
Participant 02	Standard	236	0
Participant 03	Standard	321	0
Participant 04	Standard 1	212	0
Participant 05	Standard	267	0
Participant 06	Standard	334	0
Participant 07	Standard	287	0
Participant 08	Standard	259	0
Participant 09	Prediction ✓	246	1
Participant 10	Prediction	213	1
Participant 11	Prediction	265	1
Participant 12	Prediction 2	189	1
Participant 13	Prediction	201	1
Participant 14	Prediction	197	1
Participant 15	Prediction	289	1
Participant 16	Prediction ✓	224	1
Participant 17	Speech-based dictation	178	2
Participant 18	Speech-based dictation	289	2
Participant 19	Speech-based dictation	222	2
Participant 20	Speech-based dictation 3	189	2
Participant 21	Speech-based dictation	245	2
Participant 22	Speech-based dictation	311	2
Participant 23	Speech-based dictation	267	2
Participant 24	Speech-based dictation	197	2

$$H_0 : \mu_1 = \mu_2 = \mu_3, \alpha = .05$$

$$3 \text{ pairwise tests: } (1 - \alpha)^3 = 0.86$$

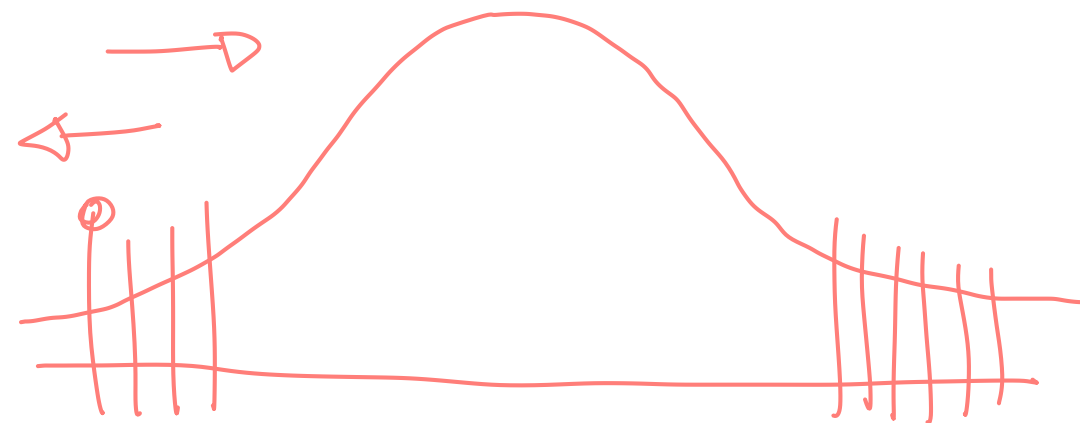
Reject  $H_0$  when  $p < 0.14$  instead of  $p < 0.05$

→ Type I error (reject  $H_0$  when it is true)

↑  
tests

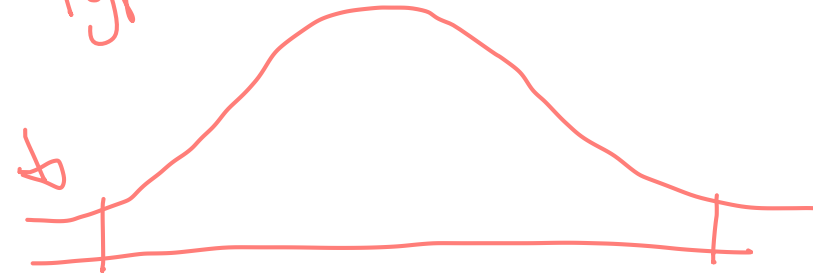
↑  
chances  
of finding  
results

\*



Type I

Type II



Participant ID	Group	Time	Coding
Participant 01	Standard	245	0
Participant 02	Standard	236	0
Participant 03	Standard	321	0
Participant 04	Standard	212	0
Participant 05	Standard	267	0
Participant 06	Standard	334	0
Participant 07	Standard	287	0
Participant 08	Standard	259	0
Participant 09	Prediction	246	1
Participant 10	Prediction	213	1
Participant 11	Prediction	265	1
Participant 12	Prediction	189	1
Participant 13	Prediction	201	1
Participant 14	Prediction	197	1
Participant 15	Prediction	289	1
Participant 16	Prediction	224	1
Participant 17	Speech-based dictation	178	2
Participant 18	Speech-based dictation	289	2
Participant 19	Speech-based dictation	222	2
Participant 20	Speech-based dictation	189	2
Participant 21	Speech-based dictation	245	2
Participant 22	Speech-based dictation	311	2
Participant 23	Speech-based dictation	267	2
Participant 24	Speech-based dictation	197	2

↙

What are errors in hypothesis testing?

Type I error: Rejecting  $H_0$  when it is true

stats error

Type II error: Accepting  $H_0$  when it is false

Type III error: Correctly rejecting  $H_0$  for the wrong reason

conceptual error

X

→

Null Hypothesis is true

Alternative Hypothesis is true

Fail to reject

Right decision

✓

Wrong decision

**Type II error** X

(False negative)

Reject

Wrong decision

**Type I error** X

(False positive)

Right decision

✓

## Analysis of Variance (ANOVA)

**Definition:** Analysis of variance (ANOVA) is a collection of statistical models and their associated estimation procedures (such as the "variation" among and between groups) used to analyze the differences among group means in a sample.<sup>1</sup>

### Procedures:

3x1

1. One-way (single factor)
2. Two-way (two factors) 2x2
3. Multi-way (multiple factors) 3x2x4

### Models:

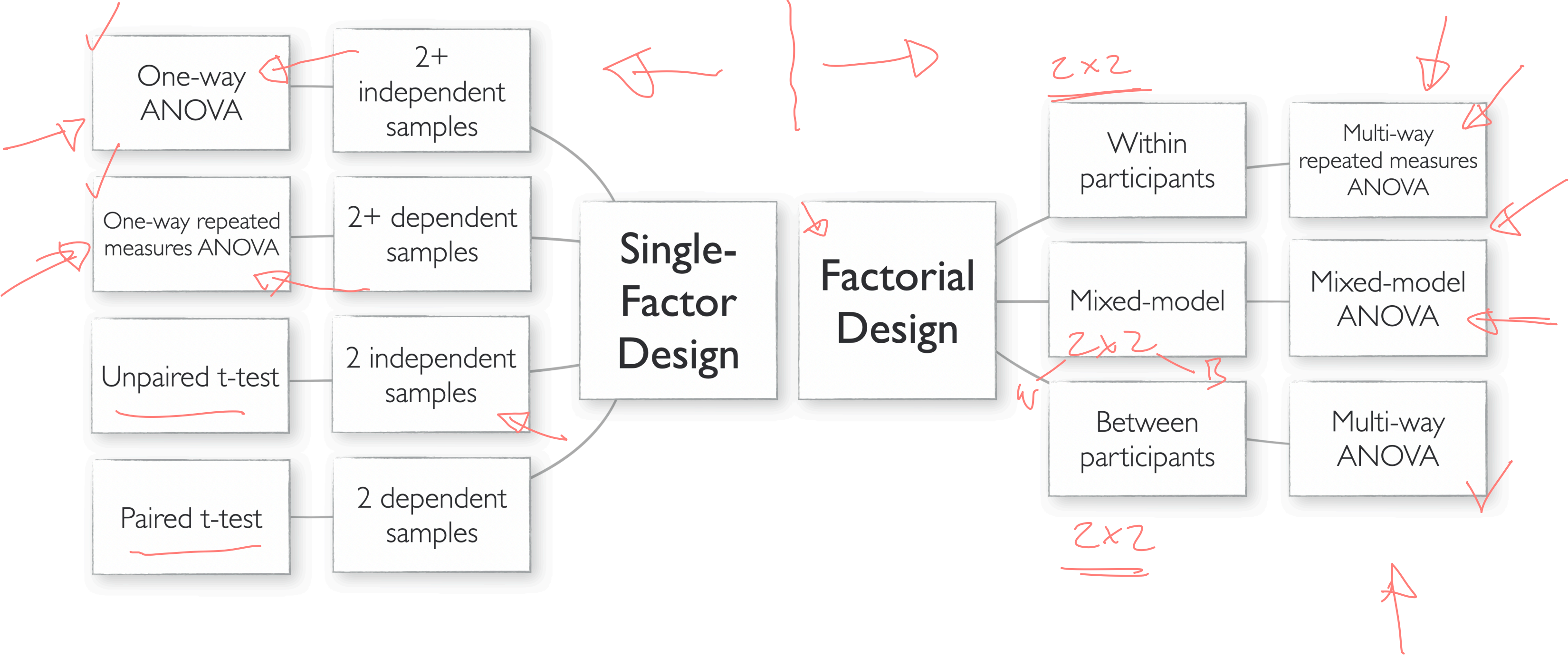
1. Fixed effects (between)
2. Random effects (within)
3. Mixed effects (mixed) W x B

---

<sup>1</sup>Wikipedia: ANOVA



How do we choose among these procedures?



How do we conduct ANOVA?

We calculate the  $F$ -statistic.

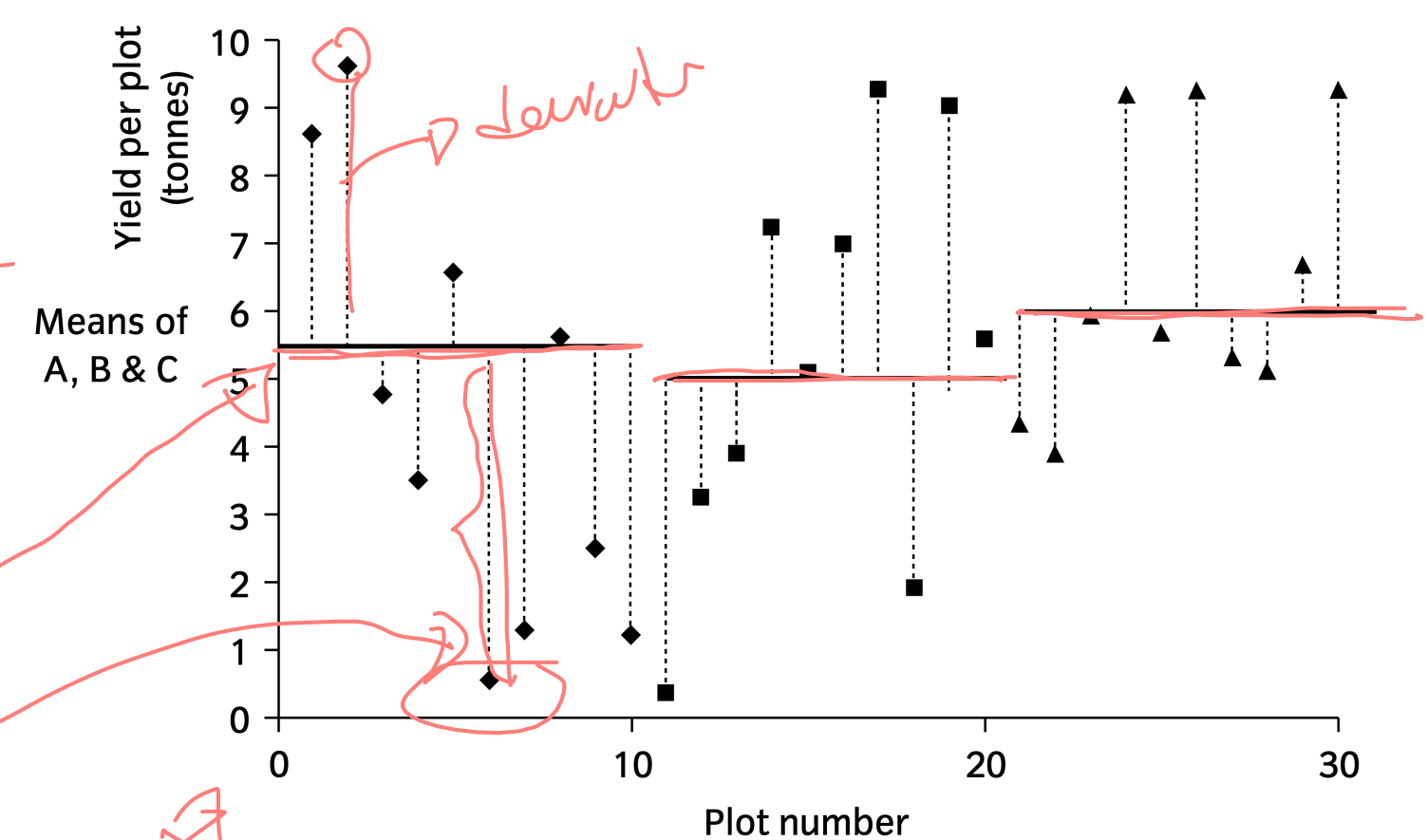
$t = \frac{\text{mean}}{\text{error}}$

24  
3x1  
 $F(2, 19) = \dots$

$$F = \frac{\sigma_{\text{explained}}}{\sigma_{\text{unexplained}}} = \frac{SS_{\text{treatment}} / (k - 1)}{SS_{\text{error}} / (n - k)}$$

*Handwritten notes:*  $3-1=2$ ,  $24-3=21$

$$F = \frac{\sum n_i (M_i - \sum (M_i/k))^2 / (k - 1)}{\sum \sum (X_{it} - M_i)^2 / (n - k)}$$



$k$ : number of populations

$n$ : sample size

# One-way ANOVA in R

```

model = aov(Time~Group,data=data)
summary(model)
    
```

DV IV

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Group	2	7842	3921	2.174	0.139
Residuals	21	37880	1804		

↓ ?

Participant ID	Group	Time	Coding
Participant 01	Standard	245	0
Participant 02	Standard	236	0
Participant 03	Standard	321	0
Participant 04	Standard	212	0
Participant 05	Standard	267	0
Participant 06	Standard	334	0
Participant 07	Standard	287	0
Participant 08	Standard	259	0
Participant 09	Prediction	246	1
Participant 10	Prediction	213	1
Participant 11	Prediction	265	1
Participant 12	Prediction	189	1
Participant 13	Prediction	201	1
Participant 14	Prediction	197	1
Participant 15	Prediction	289	1
Participant 16	Prediction	224	1
Participant 17	Speech-based dictation	178	2
Participant 18	Speech-based dictation	289	2
Participant 19	Speech-based dictation	222	2
Participant 20	Speech-based dictation	189	2
Participant 21	Speech-based dictation	245	2
Participant 22	Speech-based dictation	311	2
Participant 23	Speech-based dictation	267	2
Participant 24	Speech-based dictation	197	2

# One-way ANOVA in JMP

Analyze > Fit X by Y

**▼ Oneway Anova**

**▼ Summary of Fit**

Rsquare	0.171518
Adj Rsquare	0.092615
Root Mean Square Error	42.47149
Mean of Response	245.125
Observations (or Sum Wgts)	24

**▼ Analysis of Variance**

Source	DF	Sum of Squares	Mean Square	F Ratio	Prob > F
Group	2	7842.250	3921.13	2.1738	0.1387
Error	21	37880.375	1803.83		
C. Total	23	45722.625			

**▼ Means for Oneway Anova**

Level	Number	Mean	Std Error	Lower 95%	Upper 95%
Prediction	8	228.000	15.016	196.77	259.23
Speech-based dictation	8	237.250	15.016	206.02	268.48
Standard	8	270.125	15.016	238.90	301.35

Std Error uses a pooled estimate of error variance

$F(2, 21) = 2.1738, P = .1387$   
.05



Are we done?

The ANOVA analysis only told us whether the methods had a significant effect on *time*, not which method is more effective.

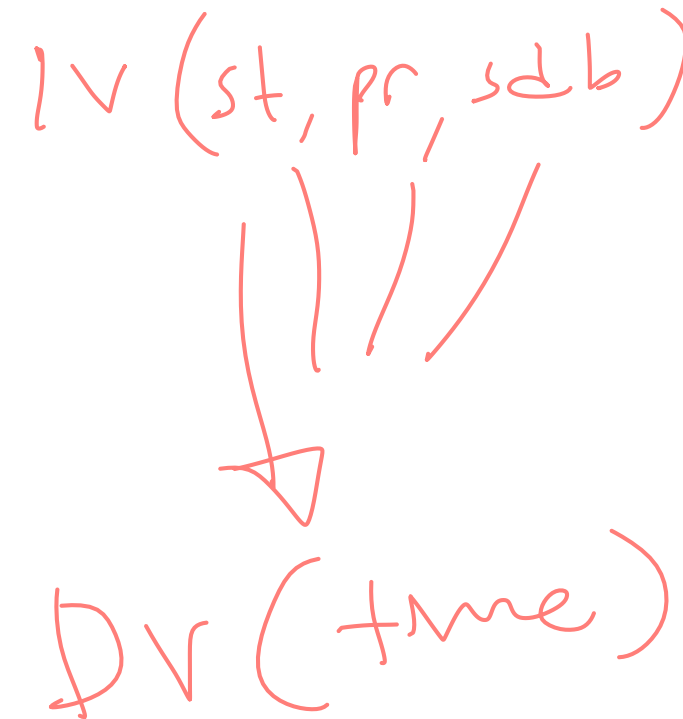
We can make two types of pairwise comparisons:

1. A priori comparisons (planned contrasts)

$$\underline{H_0: \mu_1 = \mu_2}; \underline{H_1: \mu_1 > \mu_2}$$

2. Post hoc comparisons (exploratory pairwise tests)

Test  $\mu_1$  VS  $\mu_2$ ,  $\mu_1$  VS  $\mu_3$ ,  $\mu_2$  VS  $\mu_3$



*A priori comparisons in R*

```
levels(data$Group) ✓  
comparison = c(1, -1, 0) ←  
mat = cbind(comparison)  
contrasts(data$Group) <- mat  
model = aov(Time~Group, data= data) ↓  
summary.aov(model, split = list(Group=list("mu1 vs mu2"=1)))
```

	Df	Sum Sq	Mean Sq	F	value	Pr(>F)
Group	2	7842	3921	2.174	0.139	
Group: <u>mu1 vs mu2</u>	<u>1</u>	<u>342</u>	<u>342</u>	<u>0.190</u>	<u>0.668</u>	
Residuals	21	37880	1804			

# A priori comparisons in JMP

## Compare Means > Each pair, Student's t

**Means Comparisons**

Comparisons for each pair using Student's t

**Confidence Quantile**

t	Alpha
2.07961	0.05

**LSD Threshold Matrix**

Abs(Dif)-LSD

	Standard	Speech-based dictation	Prediction
Standard	-44.162	-11.287	-2.037
Speech-based dictation	-11.287	-44.162	-34.912
Prediction	-2.037	-34.912	-44.162

Positive values show pairs of means that are significantly different.

**Connecting Letters Report**

Level	Mean
Standard	270.12500
Speech-based dictation	237.25000
Prediction	228.00000

Levels not connected by same letter are significantly different.

**Ordered Differences Report**

Level	- Level	Difference	Std Err Dif	Lower CL	Upper CL	p-Value
Standard	Prediction	42.12500	21.23574	-2.0371	86.28715	0.0605
Standard	Speech-based dictation	32.87500	21.23574	-11.2871	77.03715	0.1365
Speech-based dictation	Prediction	9.25000	21.23574	-34.9121	53.41215	0.6676

*Post hoc comparison in R*

## **TukeyHSD(model)**

**Tukey multiple comparisons of means  
95% family-wise confidence level**

**Fit: aov(formula = Time ~ Group, data = data)**

**\$Group**

	<b>diff</b>	<b>lwr</b>	<b>upr</b>	<b>p adj</b>
<b>Speech-based dictation-Prediction</b>	<b>9.250</b>	<b>-44.27619</b>	<b>62.77619</b>	<b>0.9011856</b>
<b>Standard-Prediction</b>	<b>42.125</b>	<b>-11.40119</b>	<b>95.65119</b>	<b>0.1409733</b>
<b>Standard-Speech-based dictation</b>	<b>32.875</b>	<b>-20.65119</b>	<b>86.40119</b>	<b>0.2896872</b>

# Post hoc comparison in JMP

## Compare Means > All Pairs, Tukey HSD

▼ **Comparisons for all pairs using Tukey-Kramer HSD**

▼ **Confidence Quantile**

q*	Alpha
2.52057	0.05

▼ **HSD Threshold Matrix**

Abs(Dif)-HSD

	Standard	Speech-based dictation	Prediction
Standard		-53.526	-20.651
Speech-based dictation			-53.526
Prediction			

Standard Speech-based dictation Prediction  
 Standard -53.526 -20.651 -11.401  
 Speech-based dictation -20.651 -53.526 -44.276  
 Prediction -11.401 -44.276 -53.526

Positive values show pairs of means that are significantly different.

▼ **Connecting Letters Report**

Level	Mean
Standard	A 270.12500
Speech-based dictation	A 237.25000
Prediction	A 228.00000


Levels not connected by same letter are significantly different.

▼ **Ordered Differences Report**

Level	- Level	Difference	Std Err Dif	Lower CL	Upper CL	p-Value
Standard	Prediction	42.12500	21.23574	-11.4012	95.65119	0.1410
Standard	Speech-based dictation	32.87500	21.23574	-20.6512	86.40119	0.2897
Speech-based dictation	Prediction	9.25000	21.23574	-44.2762	62.77619	0.9012

What if we had a within-participants design?

We conduct a repeated-measures or random-effects one-way ANOVA.



Participant ID	Group	Time	Coding
Participant 01	Standard ✓	245	0
Participant 01	Prediction ✓	246	1
Participant 01	Speech-based dictation ✓	178	2
Participant 02	Standard	236	0
Participant 02	Prediction	213	1
Participant 02	Speech-based dictation	289	2
Participant 03	Standard	321	0
Participant 03	Prediction	265	1
Participant 03	Speech-based dictation	222	2
Participant 04	Standard	212	0
Participant 04	Prediction	189	1
Participant 04	Speech-based dictation	189	2
Participant 05	Standard	267	0
Participant 05	Prediction	201	1
Participant 05	Speech-based dictation	245	2
Participant 06	Standard	334	0
Participant 06	Prediction	197	1
Participant 06	Speech-based dictation	311	2
Participant 07	Standard	287	0
Participant 07	Prediction	289	1
Participant 07	Speech-based dictation	267	2
Participant 08	Standard	259	0
Participant 08	Prediction	224	1
Participant 08	Speech-based dictation	197	2

Within-participants one-way ANOVA in R

*DV* *IV* + *↓* *↓*  
`model = aov(Time~Group+Error(Participant.ID/Group), data= data)  
summary(model)`

**Error: Participant.ID**

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Residuals	7	19113	2730		

**Error: Participant.ID:Group**

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Group	2	7842	3921	2.925	0.0868 .
Residuals	14	18767	1341		

---

**Signif. codes:** 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1



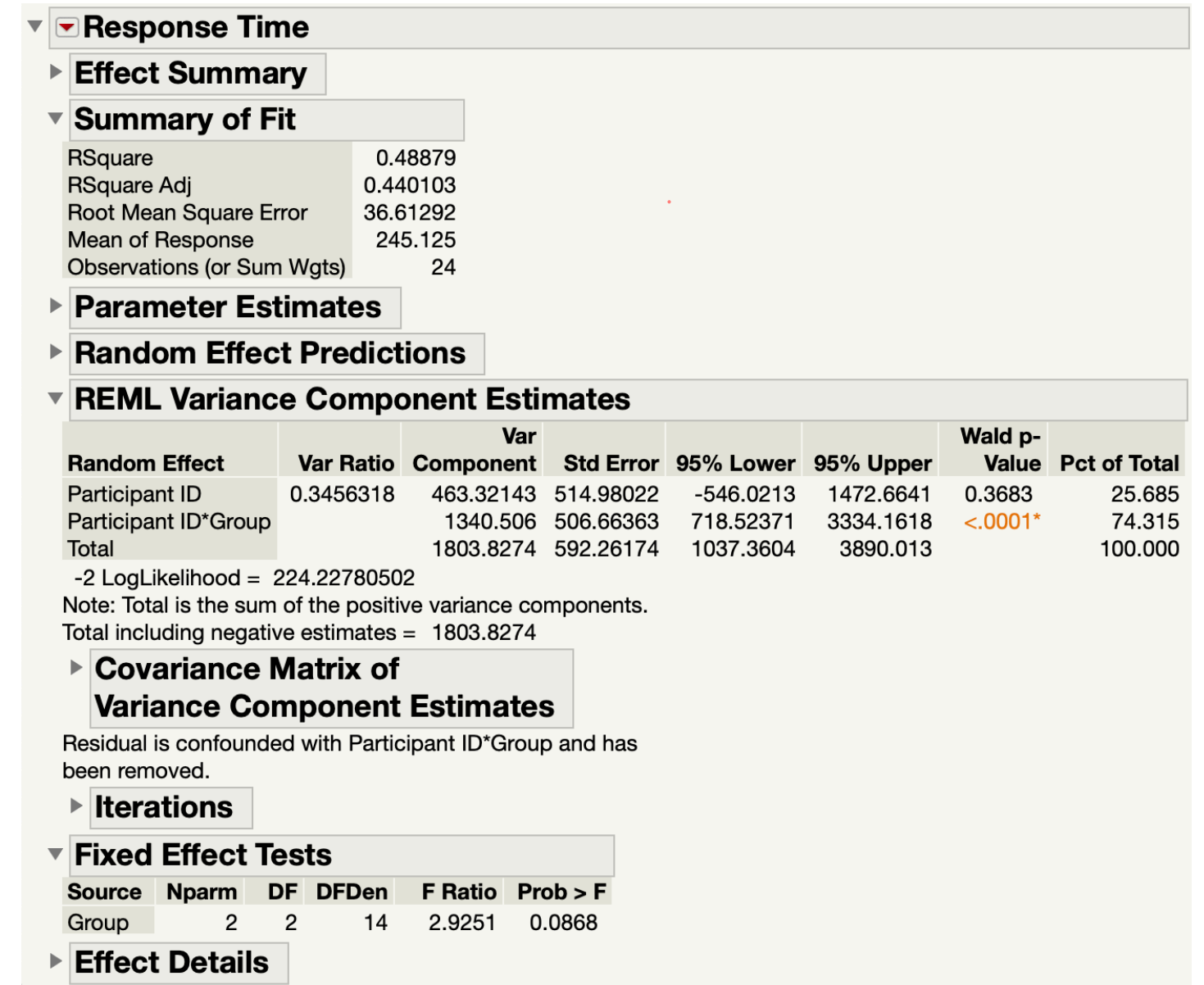
## Within-participants one-way ANOVA in JMP

### Using the Full Factorial Repeated Measures ANOVA Add-In:

Add-ins > Repeated Measures > Full-Factorial Design (Mixed Effects)

For additional options (e.g., comparisons):

Launch Dialog > Emphasis: Effect Leverage



**Response Time**

- ▶ **Effect Summary**
- ▼ **Summary of Fit**

RSquare	0.48879
RSquare Adj	0.440103
Root Mean Square Error	36.61292
Mean of Response	245.125
Observations (or Sum Wgts)	24
- ▶ **Parameter Estimates**
- ▶ **Random Effect Predictions**
- ▼ **REML Variance Component Estimates**

Random Effect	Var Ratio	Var Component	Std Error	95% Lower	95% Upper	Wald p-Value	Pct of Total
Participant ID	0.3456318	463.32143	514.98022	-546.0213	1472.6641	0.3683	25.685
Participant ID*Group		1340.506	506.66363	718.52371	3334.1618	<.0001*	74.315
Total		1803.8274	592.26174	1037.3604	3890.013		100.000

-2 LogLikelihood = 224.22780502  
Note: Total is the sum of the positive variance components.  
Total including negative estimates = 1803.8274
- ▶ **Covariance Matrix of Variance Component Estimates**

Residual is confounded with Participant ID\*Group and has been removed.
- ▶ **Iterations**
- ▼ **Fixed Effect Tests**

Source	Nparm	DF	DFDen	F Ratio	Prob > F
Group	2	2	14	2.9251	0.0868
- ▶ **Effect Details**



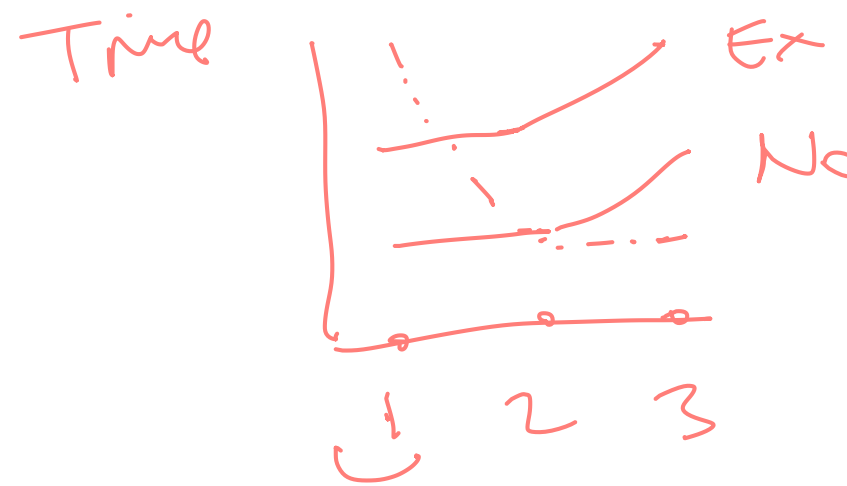
*Between-participants two-way ANOVA in R*

```
model = aov(Time~Group*Expertise, data=data)  
summary(model)
```

	<b>Df</b>	<b>Sum Sq</b>	<b>Mean Sq</b>	<b>F</b>	<b>value</b>	<b>Pr(&gt;F)</b>
<b>Group</b>	<b>2</b>	<b>7842</b>	<b>3921</b>	<b>2.175</b>	<b>0.143</b>	
<b>Expertise</b>	<b>1</b>	<b>1395</b>	<b>1395</b>	<b>0.774</b>	<b>0.391</b>	
<b>Group:Expertise</b>	<b>2</b>	<b>4030</b>	<b>2015</b>	<b>1.117</b>	<b>0.349</b>	
<b>Residuals</b>	<b>18</b>	<b>32455</b>	<b>1803</b>			

# Between-participants two-way ANOVA in JMP

Analyze > Fit Model



**Summary of Fit**

RSquare	0.290171
RSquare Adj	0.092996
Root Mean Square Error	42.46257
Mean of Response	245.125
Observations (or Sum Wgts)	24

**Analysis of Variance**

Source	DF	Sum of Squares	Mean Square	F Ratio
Model	5	13267.375	2653.48	1.4716
Error	18	32455.250	1803.07	<b>Prob &gt; F</b>
C. Total	23	45722.625		0.2477

**Parameter Estimates**

Term	Estimate	Std Error	t Ratio	Prob> t
Intercept	245.125	8.667635	28.28	<.0001*
Group[Prediction]	-17.125	12.25789	-1.40	0.1794
Group[Speech-based dictation]	-7.875	12.25789	-0.64	0.5287
Expertise[Expert]	-7.625	8.667635	-0.88	0.3906
Group[Prediction]*Expertise[Expert]	-14.625	12.25789	-1.19	0.2483
Group[Speech-based dictation]*Expertise[Expert]	16.875	12.25789	1.38	0.1855

**Effect Tests**

Source	Nparm	DF	Sum of Squares	F Ratio	Prob > F
Group	2	2	7842.2500	2.1747	0.1426
Expertise	1	1	1395.3750	0.7739	0.3906
Group*Expertise	2	2	4029.7500	1.1175	0.3488

# Within-participants two-way ANOVA in R

IV, IV1 \* IV2 +

```
model = aov(Time~(Group*Task)+Error(Participant.ID/(Group*Task)), data= data)
summary(model)
```

Participant ID	Group	Task	Time
Participant 01	Standard	Complex	285
Participant 01	Prediction	Complex	160
Participant 01	Speech-based dictation	Complex	201
Participant 01	Standard	Simple	272
Participant 01	Prediction	Simple	191
Participant 01	Speech-based dictation	Simple	161
Participant 02	Standard	Complex	189
Participant 02	Prediction	Complex	250
Participant 02	Speech-based dictation	Complex	178
Participant 02	Standard	Simple	247
Participant 02	Prediction	Simple	288
Participant 02	Speech-based dictation	Simple	180
Participant 03	Standard	Complex	233
Participant 03	Prediction	Complex	285
Participant 03	Speech-based dictation	Complex	225
Participant 03	Standard	Simple	200
Participant 03	Prediction	Simple	202
Participant 03	Speech-based dictation	Simple	162

```
Error: Participant.ID
      Df Sum Sq Mean Sq F value Pr(>F)
Residuals  7  7224    1032
```

```
Error: Participant.ID:Group
      Df Sum Sq Mean Sq F value Pr(>F)
Group   2  1650    825.2  0.345  0.714
Residuals 14 33441   2388.6
```

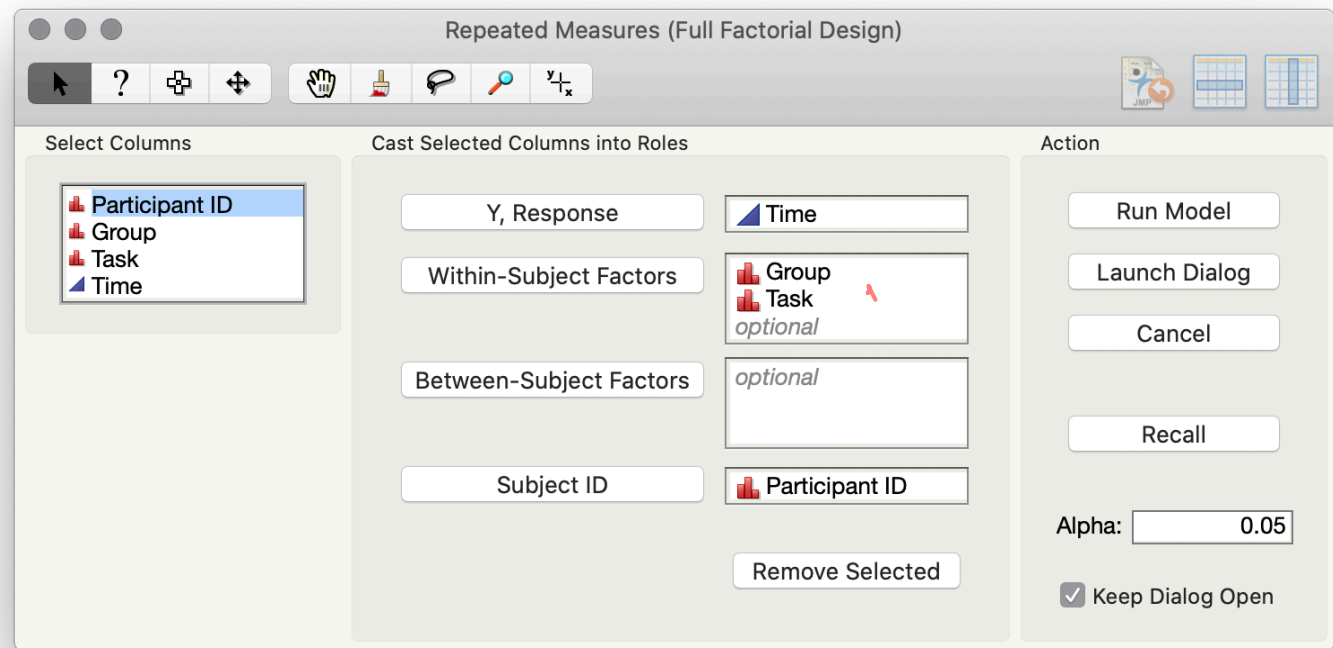
```
Error: Participant.ID:Task
      Df Sum Sq Mean Sq F value Pr(>F)
Task    1   341    341.3  0.119  0.74
Residuals  7 20055   2865.0
```

```
Error: Participant.ID:Group:Task
      Df Sum Sq Mean Sq F value Pr(>F)
Group:Task  2  1845    922.5  0.644  0.54
Residuals 14 20053   1432.3
```

# Within-participants two-way ANOVA in JMP

Add-ins > Repeated Measures > Full-Factorial Design (Mixed Effects)

*within*



**Summary of Fit**

RSquare	0.397171
RSquare Adj	0.325405
Root Mean Square Error	37.84614
Mean of Response	216.625
Observations (or Sum Wgts)	48

**Parameter Estimates**

Term	Estimate	Std Error	DFDen	t Ratio	Prob> t
Intercept	216.625	4.636889	7	46.72	<.0001*
Group[Prediction]	1.6875	9.976255	14	0.17	0.8681
Group[Speech-based dictation]	-7.875	9.976255	14	-0.79	0.4431
Task[Complex]	2.6666667	7.725769	7	0.35	0.7401
Group[Prediction]*Task[Complex]	-2.229167	7.725311	14	-0.29	0.7772
Group[Speech-based dictation]*Task[Complex]	8.4583333	7.725311	14	1.09	0.2920

**Random Effect Predictions**

**REML Variance Component Estimates**

Random Effect	Var Ratio	Component	Std Error	95% Lower	95% Upper	Wald p-Value	Pct of Total
Participant ID	-0.324559	-464.875	323.07858	-1098.097	168.34739	0.1502	0.000
Participant ID*Group	0.3338216	478.14286	526.34376	-553.4719	1509.7577	0.3637	20.022
Participant ID*Task	0.3334123	477.55655	541.42698	-583.6208	1538.7339	0.3778	19.998
Participant ID*Group*Task		1432.3304	541.36999	767.74244	3562.5512	<.0001*	59.980
Total		2388.0298	687.37698	1457.7831	4611.3193		100.000

-2 LogLikelihood = 455.15548778  
 Note: Total is the sum of the positive variance components.  
 Total including negative estimates = 1923.1548

**Covariance Matrix of Variance Component Estimates**

Residual is confounded with Participant ID\*Group\*Task and has been removed.

**Iterations**

**Fixed Effect Tests**

Source	Nparm	DF	DFDen	F Ratio	Prob > F
Group	2	2	14	0.3455	0.7138 ✓
Task	1	1	7	0.1191	0.7401 ✓
Group*Task	2	2	14	0.6441	0.5400 ✓

Split-factor

## Two-way mixed-effects ANOVA in R

IV1 IV2

```
model = aov(Time~(Group*Task)+Error(Participant.ID/Group)+Task,data=data)
```

```
summary(model)
```

W B

Participant ID	Group	Task	Time
Participant 01	Standard	Complex	285
Participant 01	Prediction	Complex	160
Participant 01	Speech-based dictation	Complex	201
Participant 02	Standard	Simple	272
Participant 02	Prediction	Simple	191
Participant 02	Speech-based dictation	Simple	161
Participant 03	Standard	Complex	189
Participant 03	Prediction	Complex	250
Participant 03	Speech-based dictation	Complex	178
Participant 04	Standard	Simple	247
Participant 04	Prediction	Simple	288
Participant 04	Speech-based dictation	Simple	180
Participant 05	Standard	Complex	233
Participant 05	Prediction	Complex	285
Participant 05	Speech-based dictation	Complex	225
Participant 06	Standard	Simple	200
Participant 06	Prediction	Simple	202
Participant 06	Speech-based dictation	Simple	162

Error: Participant.ID

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Task	1	341	341.3	0.175	0.682
Residuals	14	27279	1948.5		

Error: Participant.ID:Group

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Group	2	1650	825.2	0.432	0.654
Group:Task	2	1845	922.5	0.483	0.622
Residuals	28	53493	1910.5		



# Two-way mixed-effects ANOVA in JMP

Add-ins > Repeated Measures > Full-Factorial Design (Mixed Effects)



**Summary of Fit**

RSquare	0.057814
RSquare Adj	-0.05435
Root Mean Square Error	43.70896
Mean of Response	216.625
Observations (or Sum Wgts)	48

**Parameter Estimates**

Term	Estimate	Std Error	DFDen	t Ratio	Prob> t
Intercept	216.625	6.371352	14	34.00	<.0001*
Task[Complex]	2.6666667	6.371352	14	0.42	0.6819
Group[Prediction]	1.6875	8.922054	28	0.19	0.8513
Group[Speech-based dictation]	-7.875	8.922054	28	-0.88	0.3849
Task[Complex]*Group[Prediction]	-2.229167	8.922054	28	-0.25	0.8045
Task[Complex]*Group[Speech-based dictation]	8.4583333	8.922054	28	0.95	0.3512

**REML Variance Component Estimates**


Random Effect	Var Ratio	Component	Std Error	95% Lower	95% Upper	Wald p-Value	Pct of Total
Participant ID[Task]	0.0066379	12.681548	298.71885	-572.7966	598.15973	0.9661	0.659
Participant ID*Group[Task]		1910.4732	510.59544	1203.1556	3494.4955	<.0001*	99.341
Total		1923.1548	419.68502	1307.4704	3106.8671		100.000

-2 LogLikelihood = 457.81133323  
 Note: Total is the sum of the positive variance components.  
 Total including negative estimates = 1923.1548

**Fixed Effect Tests**

Source	Nparm	DF	DFDen	F Ratio	Prob > F
Task	1	1	14	0.1752	0.6819
Group	2	2	28	0.4319	0.6535
Task*Group	2	2	28	0.4829	0.6221

What if I would like to include a covariate?



Participant ID	Group	Time	Years
Participant 01	Standard	245	12
Participant 02	Standard	236	5
Participant 03	Standard	321	6
Participant 04	Standard	212	13
Participant 05	Standard	267	19
Participant 06	Standard	334	18
Participant 07	Standard	287	18
Participant 08	Standard	259	18
Participant 09	Prediction	246	14
Participant 10	Prediction	213	3
Participant 11	Prediction	265	19
Participant 12	Prediction	189	13
Participant 13	Prediction	201	24
Participant 14	Prediction	197	21
Participant 15	Prediction	289	5
Participant 16	Prediction	224	18
Participant 17	Speech-based dictation	178	21
Participant 18	Speech-based dictation	289	18
Participant 19	Speech-based dictation	222	23
Participant 20	Speech-based dictation	189	16
Participant 21	Speech-based dictation	245	12
Participant 22	Speech-based dictation	311	15
Participant 23	Speech-based dictation	267	16
Participant 24	Speech-based dictation	197	9

Consider the one-way between-subjects analysis and also measuring the years of experience the user had in the task to control for that factor.

We conduct what is called an analysis of covariance (ANCOVA).

One-way between-participants ANCOVA in R

```
model = aov(Time~Group+Years, data=data)
summary(model)
```

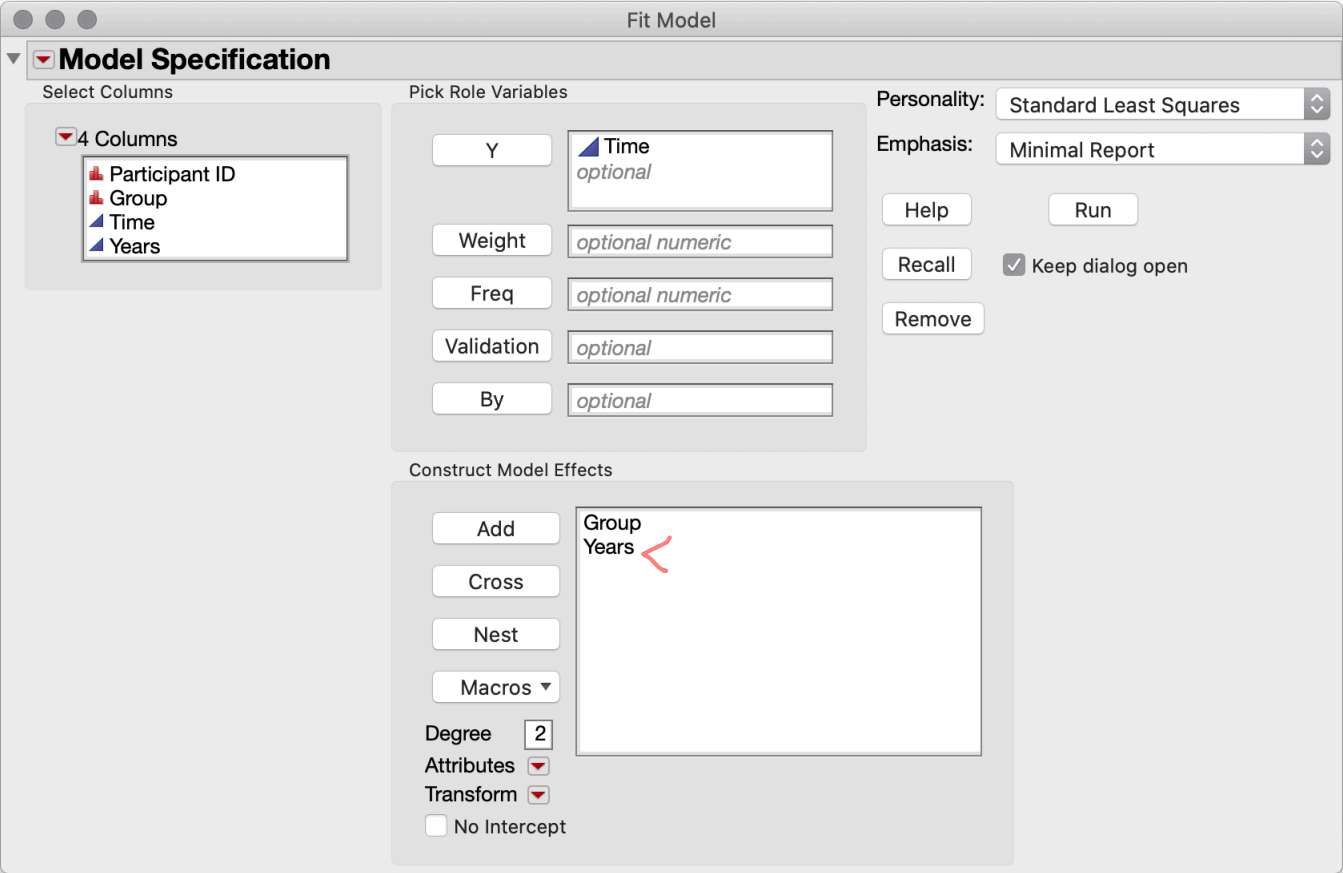
	Df	Sum Sq	Mean Sq	F value	Pr(>F)
> Group	2	7842	3921	2.090	<u>0.15</u>
> <del>Years</del>	<del>1</del>	<del>350</del>	<del>350</del>	<del>0.187</del>	<del>0.67</del>
Residuals	20	37530	1877		

Because `Years` has no effect, we would remove it from our model (called *model simplification*) and rerun our analysis as an ANOVA.



# One-way between-participants ANCOVA in JMP

Analyze > Fit Model



### Summary of Fit

RSquare	0.179172
RSquare Adj	0.056048
Root Mean Square Error	43.31881
Mean of Response	245.125
Observations (or Sum Wgts)	24

### Analysis of Variance

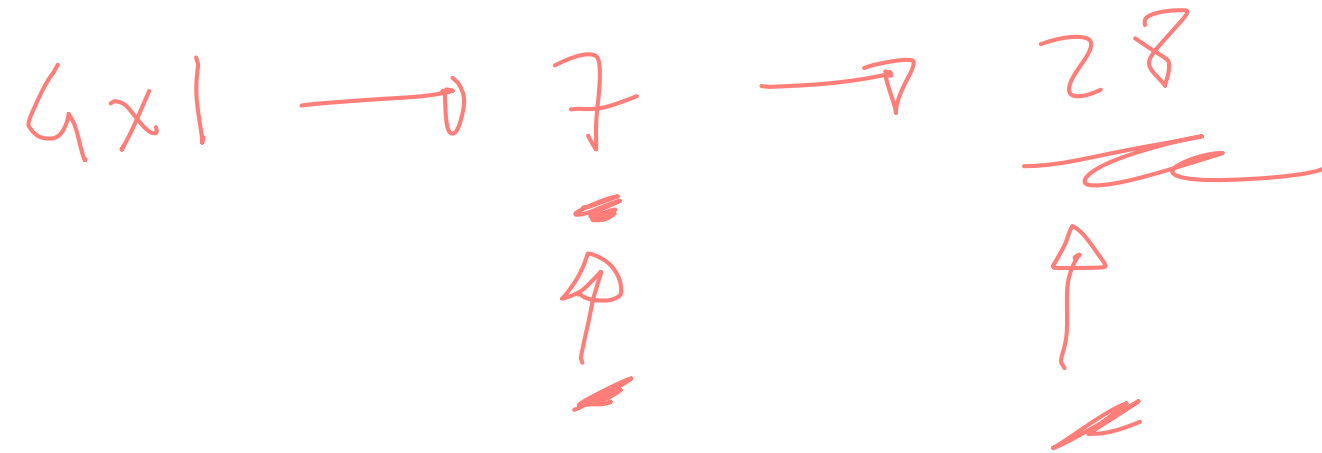
Source	DF	Sum of Squares	Mean Square	F Ratio
Model	3	8192.233	2730.74	1.4552
Error	20	37530.392	1876.52	<b>Prob &gt; F</b>
C. Total	23	45722.625		0.2568

### Parameter Estimates

Term	Estimate	Std Error	t Ratio	Prob> t
Intercept	255.22257	24.99753	10.21	<b>&lt;.0001*</b>
Group[Prediction]	-17.26682	12.50938	-1.38	0.1827
Group[Speech-based dictation]	-6.910626	12.70288	-0.54	0.5924
Years	-0.680735	1.576272	-0.43	0.6705

### Effect Tests

Source	Nparm	DF	Sum of Squares	F Ratio	Prob > F
Group	2	2	7341.1619	1.9561	0.1675
Years	1	1	349.9828	0.1865	0.6705



## Data files used in Statistics I, II, and III